EXACT SOLUTION (ANALYTICAL SOLUTION) VERSUS APPROXIMATE SOLUTION (NUMERICAL SOLUTION)

EXACT SOLUTION

 Solution that can be presented in the form of a closed-form mathematical expression

APPROXIMATE SOLUTION

 Solution that cannot be expressed in the form of mathematical expression

$$y = 2x^2 + 3x + 5$$

Evaluate
$$\frac{dy}{dx}\Big|_{x=1}$$
.

JIM 101 Calculus, Differentiation

x	0	1	2
f(x)	5	10	19

JIM 216/310 Introductory Numerical Methods, Chapter 7 Numerical Differentiation

Formula 1

$$\overline{f'(x_0)} \approx \frac{f(x_0 + h) - f(x_0)}{h}$$

Formula 2

$$f'(x_0) \approx \frac{f(x_0) - f(x_0 - h)}{h}$$

Formula 3
$$f'(x_0) \approx \frac{f(x_0 + h) - f(x_0 - h)}{2h}$$